Contents

List of Symbols IX	
Acknowledgments	XIII

1	Introduction 1 References 14					
2	Introduction to Time-Reversible, Thermostatted Dynamical Systems					
0.1	and Statistical Mechanical Ensembles 17					
2.1	Time Reversibility in Dynamical Systems 17					
2.2	Introduction to Time-Reversible, Thermostatted Dynamical Systems 19					
2.3	Example: Homogeneously Thermostatted SLLOD Equations for Planar Couette Flow 30					
2.4	Phase Continuity Equation 32					
2.5	Lyapunov Instability and Statistical Mechanics 35					
2.6	Gibbs Entropy in Deterministic Nonequilibrium					
	Macrostates 42					
2.A	Appendix: Phase Space Expansion Calculation 44 References 46					
3	The Evans – Searles Fluctuation Theorem 49					
3.1	The Transient Fluctuation Theorem 49					
3.2	Second Law Inequality 53					
3.3	Nonequilibrium Partition Identity 55					
3.4	Integrated Fluctuation Theorem 56					
3.5	Functional Transient Fluctuation Theorem 58					
3.6	The Covariant Dissipation Function 59					
3.7	The Definition of Equilibrium 60					
3.8	Conclusion 62					
0	References 63					

Contents						
4	The Dissipation Theorem 65					
4.1	Derivation of the Dissipation Theorem 65					
4.2	Equilibrium Distributions are Preserved by Their Associated Dynamics 68					
4.3	Broad Characterization of Nonequilibrium Systems: Driven, Equilibrating, and T-Mixing Systems 70					
4.3.1	Two Corollaries of the Dissipation Theorem 74 References 75					
5	Equilibrium Relaxation Theorems 77					
5.1	Introduction 77					
5.2	Relaxation toward Mixing Equilibrium: The Umbrella Sampling Approach 78					
5.3	Relaxation of Autonomous Hamiltonian Systems under T-Mixing 83					
5.4	Thermal Relaxation to Equilibrium: The Canonical Ensemble 87					
5.5	Relaxation to Quasi-Equilibrium for Nonergodic Systems 94					
5.6	Aside: The Thermodynamic Connection 94					
5.7	Introduction to Classical Thermodynamics 98					
5.A	Appendix: Entropy Change for a Cyclic Temperature Variation 104					
	References 107					
6	Nonequilibrium Steady States 109					
6 6.1	Nonequilibrium Steady States 109 The Physically Ergodic Nonequilibrium Steady State 109					
6.1	The Physically Ergodic Nonequilibrium Steady State 109					
6.1 6.2	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with					
6.1 6.2 6.3	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120					
6.1 6.2 6.3	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121					
6.1 6.2 6.3 6.4 6.5	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical					
6.1 6.2 6.3 6.4 6.5 6.6	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124					
6.1 6.2 6.3 6.4 6.5 6.6 6.7	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124					
6.1 6.2 6.3 6.4 6.5 6.6 6.7	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124 The Nonequilibrium Steady-State Fluctuation Relation 125					
6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8 6.9	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124					
6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8 6.9 6.10	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124 The Nonequilibrium Steady-State Fluctuation Relation 125 Gallavotti – Cohen Steady-State Fluctuation Relation 129					
6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8 6.9 6.10	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124 The Nonequilibrium Steady-State Fluctuation Relation 125 Gallavotti – Cohen Steady-State Fluctuation Relation 129 Summary 130					
6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8 6.9 6.10 6.11	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124 The Nonequilibrium Steady-State Fluctuation Relation 125 Gallavotti—Cohen Steady-State Fluctuation Relation 129 Summary 130 References 131					
6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8 6.9 6.10 6.11	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124 The Nonequilibrium Steady-State Fluctuation Relation 125 Gallavotti—Cohen Steady-State Fluctuation Relation 129 Summary 130 References 131 Applications of the Fluctuation, Dissipation, and Relaxation Theorems 133 Introduction 133					
6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8 6.9 6.10 6.11	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124 The Nonequilibrium Steady-State Fluctuation Relation 125 Gallavotti – Cohen Steady-State Fluctuation Relation 129 Summary 130 References 131 Applications of the Fluctuation, Dissipation, and Relaxation Theorems 133 Introduction 133 Proof of the Zeroth "Law" of Thermodynamics 134					
6.1 6.2 6.3 6.4 6.5 6.6 6.7 6.8 6.9 6.10 6.11	The Physically Ergodic Nonequilibrium Steady State 109 Dissipation in Nonequilibrium Steady States (NESSs) 111 For T-Mixing Systems, Nonequilibrium Steady-State Averages are Independent of the Initial Equilibrium Distribution 118 In the Linear Response Steady State, the Dissipation is Minimal with Respect to Variations of the Initial Distribution 120 Sum Rules for Dissipation in Steady States 121 Positivity of Nonlinear Transport Coefficients 122 Linear Constitutive Relations for T-Mixing Canonical Systems 124 Gaussian Statistics for T-Mixing NESS 124 The Nonequilibrium Steady-State Fluctuation Relation 125 Gallavotti—Cohen Steady-State Fluctuation Relation 129 Summary 130 References 131 Applications of the Fluctuation, Dissipation, and Relaxation Theorems 133 Introduction 133					

VI

7.5	Color Relaxation in Color Blind Hamiltonian Systems 147					
7.6	Instantaneous Fluctuation Relations 149					
7.7	Further Properties of the Dissipation Function 151					
	References 153					
8	Nonequilibrium Work Relations, the Clausius Inequality, and					
	Equilibrium Thermodynamics 155					
8.1	Generalized Crooks Fluctuation Theorem (GCFT) 157					
8.2	Generalized Jarzynski Equality (GJE) 161					
8.3	Minimum Average Generalized Work 164					
8.4	Nonequilibrium Work Relations for Cyclic Thermal Processes 167					
8.5	Clausius' Inequality, the Thermodynamic Temperature, and Classical					
	Thermodynamics 171					
8.6	Purely Dissipative Generalized Work 176					
8.7	Application of the Crooks Fluctuation Theorem (CFT), and the					
	Jarzynski Equality (JE) 179					
8.8	Entropy Revisited 182					
8.9	For Thermostatted Field-Free Systems, the Nonequilibrium					
	Helmholtz Free Energy is a Constant of the Motion 183					
	References 184					
	- W. 40-					
9	Causality 187					
9.1	Introduction 187					
9.2	Causal and Anti-causal Constitutive Relations 189					
9.3 Green-Kubo Relations for the Causal and Anti-causal Respon						
	Functions 190					
9.4	Example: The Maxwell Model of Viscosity 193					
9.5	Phase Space Trajectories for Ergostatted Shear Flow 194					
9.6	Simulation Results 197					
9.7	Summary and Conclusion 200					
	References 202					

Index 203