

## Index

### **a**

- AHE *see* Anomalous Hall effect (AHE)
- Angle resolved photoemission spectroscopy (ARPES) 7, 8, 162, 175, 186
  - copper-doped bismuth selenide 94
  - crystal momentum 66
  - and energy distribution curve (EDC) 218
  - Fermi surface (FS) 68, 73, 91
  - Fermi velocity 84
  - intensity maps 60
  - laser-based 70
  - momentum-dependent electronic structure, solids 219
  - and momentum distribution curve (MDC) 218
  - photoemission intensity 218
  - photon energy 59, 70
  - resistivity-temperature profile 71
  - SnTe 86
  - spectral intensity 70
  - synchrotron based 73
  - topological protection 68
- Anomalous Hall effect (AHE)
  - Chern insulator 360
  - Cr doped Sb<sub>2</sub>Te<sub>3</sub> film 369
  - electrical gate 370, 371
  - ferromagnetic order 362, 363
  - mechanism 359
- ARPES *see* Angle-resolved photoemission spectroscopy (ARPES)

### **b**

- band inversion analysis
  - DFT identification 170
  - orbital motion coupling 170
  - quasiparticle wave functions 169

- TI 170
- Bi bilayer
  - bandstructure 113
  - Bi (111) bilayer and graphene 112
  - conduction band 114, 115
  - properties 115–117
  - rhombohedral A7 structure 112
  - scanning tunneling 120
  - spin polarization 115
- Bismuth chalcogenide, TIs
  - bulk band structures 144
  - high-index surfaces 155
  - non-stoichiometric and functionalized terminations 151
  - topologically protected states 148
- bismuth-based TI materials
  - carrier concentration and surface band bending 253, 254
  - carrier density 251
  - chalcogenides 245
  - characteristics 255
  - counter-doping 254
  - crystal growth 254
  - defect properties 253
  - electrical resistivity 250, 251
  - electronic and thermodynamic phase, Bi<sub>2</sub>Se<sub>3</sub> 247
  - Fermi surfaces 251, 252
  - magnetoresistance 246
  - metallic and non-metallic specimens 255, 256
  - post-synthesis treatment 255
  - room temperature 248
  - SdH oscillations, magnetoresistance 251
  - stoichiometric Bi<sub>2</sub>Te<sub>3</sub> ratio 246
  - tetradymite *see* tetradymite
  - thermoelectric materials 246

**c**

- conductance map analysis, TIs
  - atomic scale disorder 232
  - 2D electron systems 229
  - Fourier-transformed conductance map 232
  - magnetically doped 233
  - Majorana zero mode 235
  - spin-dependent scattering probability (SSP) 230
  - superconductor 235

**d**

- Density-functional theory (DFT)
  - accuracy and computational cost 131
  - atomic wave functions 137
  - auxiliary noninteracting system 134
  - electron density gradient 136
  - electronic-structure codes 136
  - electrostatic interaction energy of nuclei 133
  - exchange-correlation energy density 135
  - and generalized-gradient approximation (GGA) 132
  - Hohenberg-Kohn theorems 134
  - ionic pseudopotentials 138
  - many-electron wave function 133
  - plane-wave pseudopotential approach 132
  - pseudopotential method 137
  - quantum-mechanical many-body problems 131
  - topological materials 131
  - ultrasoft pseudopotentials 139
- DFT calculations, TIs
  - electronic band structure parameters 136
  - electronic-structure methods 131
- Dilute magnetic semiconductors (DMS) 335, 363
- DMS *see* Dilute magnetic semiconductors (DMS)
- 2D-TIs *see* Two-dimensional TIs (2D-TIs)

**e**

- Electron energy loss spectroscopy (EELS) 317
- electronic structure, TIs
  - band inversion 163, 179
  - band-structure concept 164
  - bulk projected band structures 174, 175
  - conduction-band minimum (CBM) 162

- DFT band gap, insulators and semiconductors 161
- Dyson equation 163
- full-potential linearized augmented-plane-wave (FLAPW) formalism 166
- GW approach 164
- GWSOC 172
- LDA and GGA functionals 161
- many-body renormalization effects 163
- orbital analysis 174
- photoemission spectroscopy experiments 163
- plasmon-pole model 167
- quasiparticle band structures 163
- relativistic effects 166
- room-temperature spintronics applications 162
- topological invariants 167
- valence-band maximum (VBM) 162
- zeroth-order Green function 165
- electronic transport, TIs
  - Aharonov-Bohm (AB) effect 283–285
  - 1D electronic modes 285
  - description 279
  - Shubnikov-de Haas (SdH) oscillations 280, 282
  - superconducting proximity effect 286
  - ultrathin 283
  - weak anti-localization (WAL) 280, 281

**f**

- Ferromagnetic (FM) insulator
  - Bi-chalcogenide heterostructures 316
  - BS magnetization measurements 315
  - electrical transport measurements 320
  - hall measurements 318
  - magnetic domain switching 320
  - magnetic scattering 319
  - magnetization reversal 316
  - proximity-induced magnetism 315
  - reactive sputtering 316
  - secondary magnetic phase transition 317
  - spin-disorder scattering 316
  - time-reversal symmetry 321
  - transport devices 317
- ferromagnetism
  - conduction and valence bands 368
  - Cr doped  $(\text{Bi}_{1-x} \text{Sb}_x)_2 \text{Te}_3$  thin films 368, 370
  - Cr doped  $\text{Sb}_2 \text{Te}_3$  368
  - $\text{Sb}_2 \text{Te}_3$  and  $\text{Bi}_2 \text{Te}_3$  368
  - van Vleck mechanism 367

***g***

- graphene
  - bandstructure 107
  - 2D electron gas 107
  - electronic structure 104
  - Majorana fermions 107
  - nearest-neighbor (NN) hopping 106
  - pseudo-spin 104, 105
  - spin-orbit gap 107
  - types of hoppings 105
- GW approach
  - Bloch functions 166
  - exchange-correlation (XC) effects 164
  - Hedin's equations 165
  - nontrivial functional derivatives 165
  - optical measurements 180
  - perturbative approach 167
  - spin-independent screened interaction 165
  - spline interpolation 167

***h***

- Hall voltage 357

***i***

- inversion-asymmetric systems 15, 16

***k***

- Kitaev's model 378
- 'Klein-Majorana fusion' procedure 395
- Kohn-Sham theory 134

***l***

- LDA valence-band dispersion 176
- Local density of states (LDOS)
  - Friedel oscillations 229
  - energy-momentum dispersion 224
  - and STM 218

***m***

- magnetic and superconducting doped TIs
  - copper-doped bismuth selenide 94
  - Cu<sub>x</sub>Bi<sub>2</sub>Se<sub>3</sub> 95
  - ferromagnetism 89
  - photoemission 89
  - spin-resolved measurements 92
  - surface adsorption method 92
  - topological order 92
- magnetic doping, transition metal atoms 301
- magneto-transport experiments, HgTe quantum wells
  - magnetic-field induced phase transition 38
  - sample fabrication 36
  - transition, n-p conductance 37
- Majorana nanowires

- characteristic power-law scaling 380

- charging effects 379
- Coulomb interactions 378
- gapless surface modes 377
- interferometric detection 379
- nontrivial topological invariants 377
- quantum transport properties 378
- single-charge transistor 379
- spin-orbit coupling 378, 379
- zero-energy states 380
- Majorana single-charge transistor
  - charging energy contribution charf 383
  - charging-induced correlations 385
  - Coulomb oscillations, linear conductance 388
  - finite bias sidepeaks 389
  - functional integral approach 385
  - gauge transformation 385
  - inelastic cotunneling processes 387
  - Josephson coupling,superconducting lead 391
  - Majorana–Meir–Wingreen expression 385
  - master equation approach 386
  - noninteracting Majorana device 386
  - power-law dependence 385
  - resonant Andreev reflection to electron teleportation 389
  - sequential tunneling rates 387
  - superconducting phase fluctuations 385
  - zero-bandwidth model 386
- Majorana–Meir–Wingreen formula 381

- MBE growth, TIs

- Bi- and Sb- Chalcogenides 300
- Bi<sub>2</sub> Se<sub>2</sub> (BS) 303
- BST 305
- BT 303
- bulk HgTe 299
- carrier concentrations 298
- film growth, quality and stability 305
- ST 304
- Metal-organic chemical vapor deposition (MOCVD) 272, 299
- Molecular beam epitaxy (MBE)
  - chalcogenides 296
  - exfoliation process 298
  - massless Dirac dispersion 297
  - thermoelectric materials 296, 297
  - transport measurements 297

***p***

- probing TI surface states, STM
  - and band structure, Tis 223
  - Landau quantization 225

- probing TI surface states, STM (*contd.*)
  - sample preparation methods 219
  - topography and defects 221
  - TRS 217
- Pulsed laser deposition (PLD) 299
  
- q**
- QAHE *see* Quantum anomalous Hall effect (QAHE)
- QPT *see* Quantum phase transitions (QPT)
- QSHE *see* Quantum spin Hall effect (QSHE)
- QSHE, HgTe quantum wells
  - longitudinal resistance measurements 41
  - non-local measurements 44
  - spin polarization 45
  - transport, helical edge states 43
- Quantum anomalous Hall effect (QAHE)
  - 111, 296, 315
  - and AHE 359, 360
  - ARPES band maps,  $\text{Bi}_2\text{Se}_3$  365, 366
  - band structure, TIs 360, 363
  - $(\text{Bi}_{1-x}\text{Sb}_x)_2\text{Te}_3$  ternary compounds 366, 367
  - challenges 375
  - Cr doped  $(\text{Bi}_{1-x}\text{Sb}_x)_2\text{Te}_3$  TI films 371
  - crystal structure,  $\text{Bi}_2\text{Se}_3$  364, 365
  - electrical gate 370
  - evolution, band structure and edge states 361, 362
  - ferromagnetic (FM) order 362–364
  - ferromagnetism *see* ferromagnetism
  - Hall effect and QHE 357, 358
  - magnetic field dependence 371, 373
  - temperatures 373
  - types 374
- quantum-mechanical many-body effects 135
- Quantum phase transitions (QPT)
  - ARPES and spin-resolved ARPES 75
  - bulk band inversion, BiTI 76, 77
  - conventional band insulator 74
  - energy dispersion and FS mapping 75
  - photoemission measurements 75
- Quantum spin Hall effect (QSH) 268
  - backscattering, helical edge state 48
  - Berry-phase effects 6
  - description 3
  - graphene 4
  - HgTe/CdTe quantum wells 33
  - in InAs/GaSb quantum wells 49
  - in magnetic field 45
  - probing, edge states 48
  - quantized spin-Hall conductance 4
  - in semiconductors 32
- semiconductor quantum well (QW) 31
- spin polarization 33
- system InAs/GaSb 35
- time-reversal (TR) invariant perturbations 32
- time-reversal (TR) symmetry 31
- and TIs *see* Topological insulators (TIs)
- topological phase transition 33
- transport measurement 32
- transverse conductivity 32
  
- r**
- Reflection high energy electron diffraction (RHEED) oscillations 303
  
- s**
- Scanning gate microscopy (SGM) 48
- Scanning tunneling microscopy (STM)
  - description 218
  - single atom imaging 218
- scotch-tape method 247
- Screened-exchange LDA (sX-LDA) approach 179
- SdH oscillations *see* Shubnikov–de Haas (SdH) oscillations
- Shubnikov–de Haas (SdH) oscillations
  - amplitude 343
  - density of 2D carriers 343
  - description 340
  - 2D nature 340, 341
  - Fourier analysis 342
  - Landau-level (LL) fan diagram 341, 342
- skyrmion 110
- Spatially-resolved STS (SR-STS) 218
- SPE *see* Superconducting proximity effect (SPE)
- spin chirality, surface Dirac cones 19
- Spin-orbit coupling (SOC)
  - band gap region 161
  - band inversion 169
  - Hartree potential 164
  - LDA calculations 171
  - non-interacting reference system 163
  - spin-orbit splittings 172
  - treatment 170, 172
- Spin-orbit interaction (SOI)
  - computational requirements 142
  - Dirac equations 140
  - electronic and magnetic properties 139
  - electronic-structure calculations 141
  - first-order perturbation theory 141
  - nonrelativistic pseudopotentials 140
  - scalar-relativistic (SR) effects 139
  - semilocal pseudopotentials 141

- spinor plane-wave matrix element 142
- spinor wave functions 142
- spintronics applications 164
- Superconducting proximity effect (SPE)
  - Al-Bi<sub>2</sub>Se<sub>3</sub>-Al junction 349, 351
  - Bi<sub>2</sub>Se<sub>3</sub>-(Bi-2212) junctions 352, 353
  - differential resistance  $dV/dI$  346
  - Josephson effect, Nb-Bi<sub>2</sub>Te<sub>3</sub>-Nb junctions 348
  - Majorana fermions 344
  - Nb-HgTe-Nb junction 350
  - Sn-Bi<sub>2</sub>Se<sub>3</sub> and Pb-Bi<sub>2</sub>Ses junctions 346
  - temperatures, Sn-Bi<sub>2</sub>Se<sub>3</sub> 344, 345
  - W-Bi<sub>2</sub>Se<sub>3</sub>-W junction 347
- surface electronic structure, TIs and TCIs
  - ARPES and STM techniques 191
  - bismuth and antimony 200, 202
  - chalcogenites 198, 200
  - Fermi energy 198
  - mirror symmetry 204, 206
  - PbTe and SnTe 204, 205
  - scattering 207, 208
  - spin-degeneration 197
  - stability, surface states' existence 208, 209, 211
  - topological predictions 196
  - TRIMs *see* Time-reversal invariant momenta (TRIMs)

## t

- TDS *see* Topological Dirac semimetals (TDS)
- tetradymite
  - chemical substitution and defects 249
  - melting powder 248
  - polycrystalline masses 246
  - rhombohedral crystal structure 247
  - SdH oscillations 250
  - transport measurements 250
- thin-film synthesis techniques 249
- TI nanostructures
  - applications 286, 288
  - description 267
  - doping and alloy 275, 276
  - exfoliation 273
  - fermi level modulation and bulk carrier control 276, 278
  - heterostructures 274
  - opportunities enabled 270
  - solution phase growth 273
  - vapor phase growth 271, 272
- Time-reversal invariant momenta (TRIMs)
  - 170
  - definition 192
  - Fermi contours 195

- inversion symmetry 193
- parity invariants 193, 194
- surface Brillouin zone (SBZ) 194, 195
- surface state topology 194
- Time reversal symmetry (TRS) 217
- TIs. *see* Topological insulators (TIs)
- TIs, magnetism
  - bulk ferromagnetism 313
  - FM/TI heterostructures 315
- TKI *see* Topological Kondo insulator (TCI)
- Topological crystalline insulator (TCI)
  - band inversion transition 86
  - GeBi<sub>2</sub>Te<sub>4</sub> 87
  - Pb<sub>x</sub>Sn<sub>1-x</sub>Te 85
  - protection, time-reversal symmetry 85
  - scanning tunneling spectroscopies 89
  - spin polarization 85
  - spin-resolved ARPES measurements 87
  - surface band dispersion 88
  - van Hove singularity (VHS) 87
- Topological Dirac semimetals (TDS)
  - arsenic ions 80
  - bulk conduction and valence bands 84
  - chemical composition delta 84
  - constant energy contour maps 82
  - Fermi level 80
  - graphene 76
  - mobility 84
  - Pauli matrices 79
  - spin-orbit coupling 80
  - surface electronic structure of 2D and 3D 83
  - tetragonal structure 81
  - topological phase transition 79
  - Weyl fermions 79
- Topological insulators (TIs)
  - ARPES 295
  - band structures 257
  - band structures, materials 61
  - bismuth *see* bismuth-based TI materials
  - bismuth-antimony alloy system 58, 59
  - bismuth selenide (Bi<sub>2</sub>Se<sub>3</sub>) 268
  - CdTe/HgTe/CdTe quantum 4, 5
  - chalcogenide 257
  - chalcogenide materials 269
  - chemical potential, Dirac point 67
  - crystals of SmB<sub>6</sub> 259
  - density, helical Dirac electrons 68
  - 2D HgTe quantum wells 245
  - discovery 8
  - dispersion, interface 23
  - electrical/optical method 353
  - electron transport 268
  - electronic phases 3

- Topological insulators (TIs) (*contd.*)
  - electronics applications 267
  - energy gaps 257
  - experimental discovery of 3D 57
  - fabrication process 298
  - gapless states, interface 22
  - half-Heusler *RTX* compounds 257
  - half-Heusler materials 257, 258
  - helical spin texture 64
  - heterostructures 315
  - Heusler materials 6
  - ionic liquid gating 298
  - IQH, FQH and QSH 55
  - Kondo insulator 259
  - magnetism/superconductivity 296
  - material quality 7
  - mirror symmetries, crystalline 67
  - nanostructures *see* TI nanostructures
  - non-metallic behavior 258
  - non-zero Berry's phase, Fermi surface (FS) 61
  - photo-induced band-gaps, graphene 8
  - photon energy 59
  - physical properties 63
  - quantized hall conductance 296
  - quantum oscillations 340, 341, 343
  - Rashba splitting, surface states 24
  - room temperature 64, 66
  - skipping orbits 56
  - SPE *see* Superconducting proximity effect (SPE)
  - spin-ARPES 58, 63
  - spin-momentum interlocking 267
  - spin-orbit coupling 7, 295
  - spin polarization 66
  - spin properties 61, 63
  - spin-resolved ARPES 331
  - spintronic device configurations 295
  - superlattice 25
  - surface energy bands 24
  - surface oxidation and mobility degradation 269
  - surface states and electronic band dispersion 59, 60
  - tetradymite *see* tetradymite
  - thermoelectric properties 8
  - thin film 20
  - three dimensional, graphene 5, 6
  - three-dimensional topological order 57
  - time-reversal invariant momenta (TRIM) 12
  - topological invariants 57
  - topological order 62
  - two dimensions (2D) *see* Quantum spin hall effect (QSHE)
  - WAL *see* Weak anti-localization (WAL)
  - and Weyl semimetals, phase transition 15
- topological invariants
  - deformation process 144
  - inversion symmetry 144
  - numerical approaches 144
  - time-reversal invariant momenta 143
- topological Kondo effect
  - bosonization approach 396
  - conductance tensor 396
  - fixed point 395
  - low-energy theory 393
  - Majorana spin 394
  - renormalization group analysis 394
- Topological Kondo insulator (TKI)
  - CsCl-type structure 70
  - Fermi surface map 73, 74
  - heavy fermion behavior 69
  - laser-based ARPES system 70
  - photon energy, laser-ARPES 73
  - surface-sensitive transport measurements 69
  - temperatures 70, 73
- topological phases 55
- topological phases and surface states
  - band structures 11
  - chirality 11
  - nontrivial transition 12
  - pair annihilation 18
  - Weyl semimetals 13
- Topological surface states (TSSs) 217
- transport studies, TI thin films
  - charged impurity disorder 307
  - hall effect 307
  - hybridization gaps, Ultrathin 3D TI films 311
  - lattice mismatch 307
  - mesoscopic transport, 3D TI films 310
  - QC, diffusive transport in 3D TI Films 309
  - QSH effect 306
  - Shubnikov-de Haas (SdH) oscillations 308
  - spin polarizations 307
- transport, Majorana nanowires
  - conductance, non-interacting 382
  - Majorana-Meir-Wingreen formula 381
  - Majorana single-charge transistor 380
- Troullier-Martins scheme 139
- Two-dimensional TIs (2D-TIs)
  - alloyed layers, Bi and Sb 118, 119
  - Bi bilayer *see* Bi bilayer
  - binary compounds 122, 123
  - bismuth and mercury compounds 104

- Chern number 111
- 2D Dirac equation 108
- Dresselhaus effect 112
- graphene and QSHE *see* grapheme
- Hamiltonian properties 110
- Luttinger-Kohn Model 109
- mass-velocity 109
- material-dependent parameters 110
- semiconductors 103
- skyrmion 110
- spin channel 109
- surface bands 103
- ternary compounds 124, 125
- topological description 111

**v**

- valence band dispersion 176
- Vapor liquid solid (VLS) methods 299

**w**

- WAL *see* Weak anti-localization (WAL)
- Weak anti-localization (WAL)
  - Cr-doped  $\text{Bi}_2\text{Se}_3$  films, magnetoconductivity curves 335, 336
  - gate voltage 337, 338
  - HLN equation 332

- impurity effect 333
- magnetoconductivity, 10 nm  $\text{Bi}_2\text{Se}_3$  332
- magnetoresistance (MR) measurement 332
- monolayer (ML) Fe deposition 333, 335
- nanowires 339
- normalized magnetoresistance,  $\text{Bi}_2\text{Te}_3$  333, 334
- phase coherent length 339
- SdH oscillation 336
- surface electron 331
- ultra-thin  $\text{Bi}_2\text{Se}_3$  films 336
- Weyl semimetals
  - apex, Dirac cone 13
  - 2D Dirac semimetal 15
  - Fermi arc surface states 13
  - inversion symmetry 15
  - time-reversal symmetry 15
  - and topological insulators, phase transition 15
  - topological nature 13

**x**

- X-ray magnetic circular dichroism (XMCD) 314

