

Contents

Preface *XI*

Abbreviations and Symbols *XV*

Color Plates *XXI*

Part One Theoretical Aspects of Superconductivity in 1D Nanowires 1

1 Superconductivity: Basics and Formulation 3

1.1 Introduction 3

1.2 BCS Theory 4

1.3 Bogoliubov–de Gennes Equations – Quasiparticle Excitations 8

1.4 Ginzburg–Landau Theory 10

1.4.1 Time-Dependent Ginzburg–Landau Theory 12

1.5 Gorkov Green’s Functions, Eilenberger–Larkin–Ovchinnikov Equations, and the Usadel Equation 12

1.6 Path Integral Formulation 19

References 27

2 1D Superconductivity: Basic Notions 31

2.1 Introduction 31

2.2 Shape Resonances – Oscillations in Superconductivity Properties 33

2.2.1 Early Treatments of Shape Resonances in 2D Films 35

2.2.2 Bogoliubov–de Gennes Equations, Finite Temperature, and Parabolic-Band Approximation for Realistic Materials 40

2.2.3 Numerical Solutions and Thin Film Shape Resonances 42

2.2.4 1D Nanowires – Shape Resonances and Size Oscillations 45

2.3 Superconductivity in Carbon Nanotubes – Single-Walled Bundles and Individual Multiwalled Nanotubes 48

2.4 Phase Slips 50

2.4.1 Finite Voltage in a Superconducting Wire and Phase Slip 51

2.4.2 Phase Slip in a Josephson Junction 52

2.4.3 Langer–Ambegaokar Free Energy Minima in the Ginzburg–Landau Approximation 55

2.4.4 Transition Rate and Free Energy Barrier 59

2.4.5	Free Energy Barrier for a Phase Slip in the Ginzburg–Landau Theory	60
2.4.6	Physical Scenario of a Thermally-Activated Phase Slip	64
2.4.7	McCumber–Halperin Estimate of the Attempt Frequency	66
	References	71
3	Quantum Phase Slips and Quantum Phase Transitions	75
3.1	Introduction	75
3.2	Zaikin–Golubev Theory	79
3.2.1	Derivation of the Low Energy Effective Action	80
3.2.2	Core Contribution to the QPS Action	88
3.2.3	Hydrodynamic Contribution to the Phase-Slip Action	91
3.2.4	Quantum Phase-Slip Rate	92
3.2.5	Quantum Phase-Slip Interaction and Quantum-Phase Transitions	95
3.2.6	Wire Resistance and Nonlinear Voltage–Current Relations	97
3.3	Short-Wire Superconductor–Insulator Transition: Büchler, Geshkenbein and Blatter Theory	100
3.4	Refael, Demler, Oreg, Fisher Theory – 1D Josephson Junction Chains and Nanowires	105
3.4.1	Discrete Model of 1D Josephson Junction Chains	107
3.4.2	Resistance of the Josephson Junctions and the Nanowire	114
3.4.3	Mean Field Theory of the Short-Wire SIT	116
3.5	Khlebnikov–Pryadko Theory – Momentum Conservation	121
3.5.1	Gross–Pitaevskii Model and Quantum Phase Slips	123
3.5.2	Disorder Averaging, Quantum Phase Transition and Scaling for the Resistance and Current–Voltage Relations	126
3.5.3	Short Wires – Linear QPS Interaction and Exponential QPS Rate	130
3.6	Quantum Criticality and Pair-Breaking – Universal Conductance and Thermal Transport in Short Wires	136
	References	143
4	Duality	149
4.1	Introduction	149
4.2	Mooij–Nazarov Theory of Duality – QPS Junctions	152
4.2.1	QPS Junction Voltage-Charge Relationship and Shapiro Current Steps	156
4.2.2	QPS Qubits	157
4.3	Khlebnikov Theory of Interacting Phase Slips in Short Wires: Quark Confinement Physics	159
	References	165
5	Proximity Related Phenomena	167
5.1	Introduction	167
5.2	Transport Properties of Normal-Superconducting Nanowire-Normal (N-SCNW-N) Junctions	169
5.2.1	Nonequilibrium Usadel Equations	169
5.2.2	Parameterization of the Usadel Equations	174

- 5.2.3 Numerical Results 175
- 5.3 Superconductor–Semiconductor Nanowire–Superconductor Junctions 179
- 5.4 Majorana Fermion in S-SmNW-S Systems with Strong Spin–Orbit Interaction in the Semiconductor 184
- References 188

Part Two Review of Experiments on 1D Superconductivity 193

6 Experimental Technique for Nanowire Fabrication 195

- 6.1 Experimental Technique for the Fabrication of Ultra Narrow Nanowires 195
- 6.2 Introduction to the Techniques 196
 - 6.2.1 Lithography 197
 - 6.2.2 Metal Deposition 198
 - 6.2.3 Etching 199
 - 6.2.4 Putting It All Together 199
- 6.3 Step-Edge Lithographic Technique 201
- 6.4 Molecular Templating 202
- 6.5 Semiconducting Stencils 205
- 6.6 Natelson and Willet 205
- 6.7 SNAP Technique 206
- 6.8 Chang and Altomare 208
- 6.9 Template Synthesis 209
- 6.10 Other Methods 211
 - 6.10.1 Ion Beam Polishing 211
 - 6.10.2 Angled Evaporation 213
 - 6.10.3 Resist Development 213
- 6.11 Future Developments 214
- References 216

7 Experimental Review of Experiments on 1D Superconducting Nanowires 219

- 7.1 Introduction 219
- 7.2 Filtering 220
- 7.3 Phase Slips 221
- 7.4 Overview of the Experimental Results 223
 - 7.4.1 Giordano’s Experiments 225
 - 7.4.2 Recent Experiments on QPS 226
 - 7.4.3 QPS Probed via Switching Current Measurements 239
- 7.5 Other Effects in 1D Superconducting Nanowires 248
 - 7.5.1 S-Shaped Current–Voltage Characteristic 248
- 7.6 Antiproximity Effect 250
 - 7.6.1 Stabilization of Superconductivity by a Magnetic Field 253
 - 7.6.2 Shape Resonance Effects 255
- References 257

8	Coherent Quantum Phase Slips	263
8.1	Introduction	263
8.2	A Single-Charge Transistor Based on the Charge-Phase Duality of a Superconducting Nanowire Circuit	263
8.3	Quantum Phase-Slip Phenomenon in Ultranarrow Superconducting Nanorings	266
8.4	Coherent Quantum Phase Slip	267
8.5	Conclusion	272
	References	273
9	1D Superconductivity in a Related System	275
9.1	Introduction	275
9.2	Carbon Nanotubes	275
9.2.1	Proximity Effects in SWNT	276
9.2.2	Intrinsic Superconductivity in SWNT	278
9.2.3	Superconductivity in Ropes Mediated by the Environment	281
9.3	Majorana Experiments	286
9.3.1	Majorana Experiment in Semiconducting Nanowires	286
9.3.2	Majorana Experiment in Hybrid Superconductor-Topological Insulator Devices	290
9.4	Superconducting Nanowires as Single-Photon Detectors	292
	References	297
10	Concluding Remarks	301
	Index	303